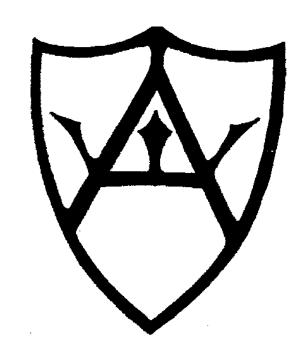
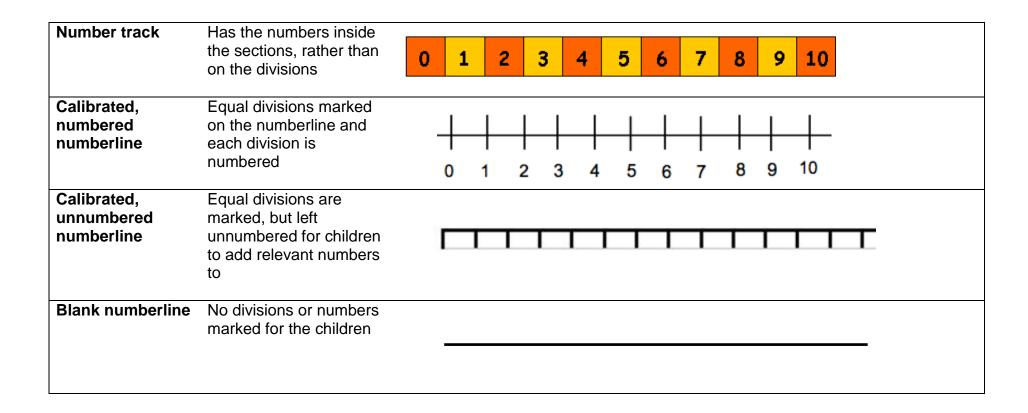
Alfriston School



Whole School Written Calculation Policy January 2015

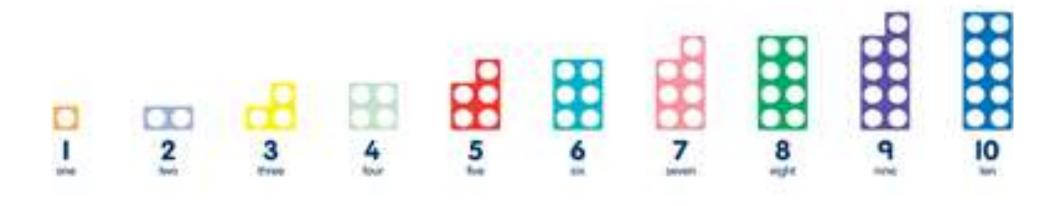
Pencil and paper procedures Key Stages 1 and 2

PROGRESSION OF NUMBERLINES



Using Numicon to support the teaching and learning of mathematics.
Use Numicon to support the models and images for the 4 operations of number.





Addition			
Stage 1	Stage 2	Stage 3	
+ = signs and missing numbers $3 + 4 = \square \qquad \square = 3 + 4$	+ = signs and missing numbers Extend to 14 + 5 = 10 + □ and adding three numbers	+ = signs and missing numbers Partition into tens and ones and recombine	
$3 + \square = 7$ $7 = \square + 4$ $\square + 4 = 7$ $7 = 3 + \square$ $\square + \nabla = 7$ $7 = \square + \nabla$	and adding three numbers 32 + □ + □ = 100 35 = 1 + □ + 5 Partition into tens and ones and recombine	Partition into tens and ones and recombine Partition both numbers and recombine. Refine to partitioning the second number only e.g. 36 + 53 = 53 + 30 + 6	
3 + 4 is the same as 7 as modelled using Numicon	12 + 23 = 10 + 2 + 20 + 3 = 30 + 5 = 35	= 83 + 6 = 89	
	refine to partitioning the second number only: 23 + 12 = 23 + 10 + 1 + 1 = 33 + 1 + 1	+30 +6	
		53 83 89 Add a near multiple of 10 to a two-digit number	

To use Numicon to further understand the equivalence in a number sentence.

(Use a picture to show what I mean)

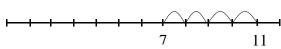
Promoting covering up of operations and numbers.

Number lines (blank)

Using blank number lines

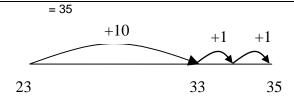
(Teacher model number lines with missing numbers)

$$7 + 4 = 11$$



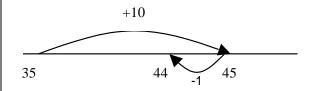
Children go up in 1s

Secure Stage 1 – able to use a hundred square



Mental Method

Add 9 or 11 by adding 10 and adjusting by 1 35 + 9 = 44



Partition into hundreds, tens and ones and recombine

Either partition both numbers and recombine or partition the second number only e.g. 358 + 73 = 358 + 70 + 3

Addition		
Stage 4	Stage 5	Stage 6

Pencil and paper procedures

83 + 42 = 125

Partition both numbers 36 = 30 + 6 43 = 40 + 3 79 = 70 + 9Recombine to get the 30+40 6+3

Leading to

Adding 3 digit numbers using the expanded method.

$$\frac{35 = 30 + 5}{184 = 100 + 70 + 14}$$
 Make sure you line up the H,TU

Pencil and paper procedures

Leading to formal method, showing numbers carried underneath

Column Addition

Column Addition will be taught alongside the Expanded Method to encourage children to see how they relate.

$$|23 = 100 + 20 + 3 | \text{sthe} | 123 \\
+ 45 = 40 + 5 | \text{same as:} + 45$$
> $|68 = 100 + 60 + 8| | 168$

Column Addition with carrying

Remember to
$$\frac{467}{100}$$
 tine up the HTV. $\frac{467}{682}$ we have to carry the $\frac{682}{100}$ we have to carry the

Extend to numbers with at least four digits 3587 + 675 = 4262

Extend to decimals (same number of decimals places) and adding several numbers (with different numbers of digits). *Model negative numbers using a number line.*

Column Addition.

Children should be comfortable with using column addition to add 4 digit numbers and several numbers with different numbers of digits at the same time.

Adding decimals using column addition. $7 \ 0.10$ 35.2 Add '0' as a place holder the line. 16.0

Subtraction		
Stage 1	Stage 2	Stage 3

Pictures / marks

Sam spent 4p. What was his change from 10p?





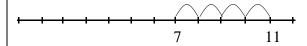
- = signs and missing numbers

7 - 3 = □	□ = 7 - 3
7 - □ = 4	4 = □ - 3
□ - 3 = 4	4 = 7 - □
\Box - ∇ = 4	4 = □ - ▽

Visual / practical activities **Number lines**

The difference between 7 and 11 (Counting on)

To reinforce concept. Practical strategies essential to see 'difference'.



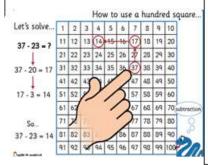
Recording by - drawing jumps on prepared lines - constructing own lines, if appropriate

(Teachers model jottings appropriate for larger numbers)

- = signs and missing numbers

Continue using a range of equations as in Stage 1 but with appropriate numbers.

Usina a Hundred Sauare:



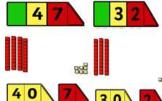
When children are ready to subtract larger numbers they will do so on a hundred square.

They will be encouraged to up in jumps of 10s and back in jumps of units.

Children are encouraged to then record this as a sum.

Leading to:

47 - 32 =



40 - 30 = 107 - 2 = 510 + 5 = 15

When children are confident in using a hundred square and have a good understanding of place value, they can then begin to partition.

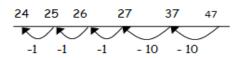
This involves partitioning the numbers into 10s and units and subtracting these. Then recombining the 10s and units to get an answer.

Children will begin to use blank number lines to support calculations.

Counting back

First counting back in tens and then in ones.

$$47 - 23 = 24$$



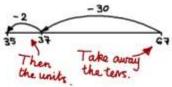
Find a small difference by counting up

Continue as in Stage 2 but with appropriate numbers e.g. 102 - 97 = 5

Counting back using a number line.

We will be using a number fine to count back from the biggest number using partitioning to help.



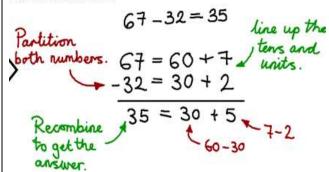


Note: Counting back is not always the most efficient method when the numbers are closer together.

Subtraction

The Expanded Method of Subtraction.

Partitioning both numbers leads to the opportunity to use more formal methods of subtraction.



The Expanded Method of Subtraction with carrying.

$$62 = 50 + 12$$
 We exchange Write these $-35 = 30 + 5$ 1 ten for numbers above. $27 = 20 + 7$ 10 units.

Pencil and paper procedures

Find a difference by counting on

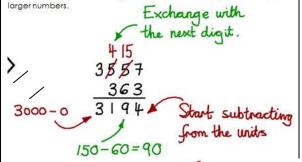
e.g. 8006 - 2993 = 5013

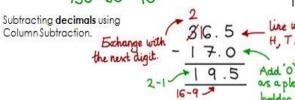
This can be modelled on an empty number line

Develop the stages of decomposition introducing 'zero'

Column Subtraction.

Children will move on to using Column Subtraction on its own and with





Develop the use of decomposition

extend to up to 2 decimal places

extend to up to 3 decimal places if appropriate

Multiplication

Stage 1

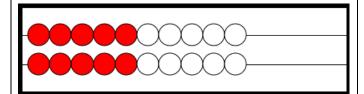
Pictures and symbols

There are 3 sweets in one bag. How many sweets are there in 5 bags?



(Recording on a number line modelled by the teacher when solving problems)

Use of bead strings to model groups of.



Use cubes and pegs. Begin to learn 2, 5 and 10 times tables.

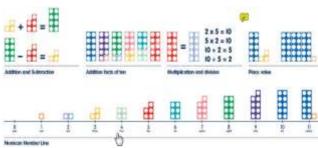
Stage 2

x = signs and missing numbers

$$7 \times 2 = \square$$
 $\square = 2 \times 7$
 $7 \times \square = 14$ $14 = \square \times 7$

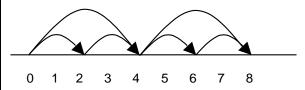
Arrays and repeated addition





2 x 4 or repeated addition

$$2 + 2 + 2 + 2$$



Doubling multiples of 5 up to 50

$$15 \times 2 = 30$$

Partition

$$(10 \times 2) + (5 \times 2)$$

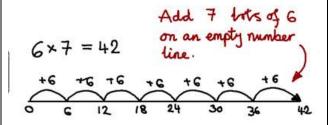
 $20 + 10 = 30$

Stage 3x = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

Repeated addition using a number line.

Understanding multiplication as repeated addition is key to understanding formal methods of multiplication.



 $35 \times 2 = 70$

Partition using Grid Method

Multiplication		
Stage 4	Stage 5	Stage 6
Stage 4 Pencil and paper procedures Grid method TU X U 23×7 is approximately $20 \times 10 = 200$ $23 \times 7 = 161$ T U X $20 \mid 3$ 7 $140 \mid 21$ HTU x U $123 \times 3 = 369$ X $100 \mid 20 \mid 3$ 3 $300 \mid 60 \mid 9$	·	Stage 6 x = signs and missing numbers Pencil and paper procedures Grid method Estimate and check Multiplying larger numbers using the Grid Method. Children will go on to multiply 2-digit by 2-digit numbers using the Grid Method. Children need to be secure in their place value and knowledge of multiplication of multiples of 10 and 100. $56 \times 43 = 2408$ Partition $56 \times 43 = 2408$ Recombine the rows $50 \times 43 = 2408$ Partition $50 \times 43 = 2408$ Recombine the rows $50 \times 43 = 2408$ Recombine the rows $50 \times 43 = 2408$ Multiply the top numbers by $50 \times 43 = 2408$ Multiply the top numbers by $50 \times 43 = 2408$ Multiply the top numbers by $50 \times 43 = 2408$ Multiply the top numbers by $50 \times 43 = 2408$ Add to get the total. Grid method for decimals Multiplying decimal numbers using the grid method. $50 \times 43 = 2408$ Add to get the total. Take care $50 \times 43 = 2408$ Add to get the total. $50 \times 43 = 2408$ 2408 Add to get the total. $50 \times 43 = 2408$ 2408 Add to get the total. $50 \times 43 = 2408$ 2408 Add to get the total.

Expanded vertical column multiplication:

Expanded with partial products

To support understanding and progression the grid method, expanded and compact methods should be shown side-by-side to emphasise the links between the different formats.

To support understanding and progression the grid method, expanded and compact methods should be shown side-by-side to emphasise the links between the different formats.

Key elements:

- Working RIGHT to LEFT
- The language of place value

Accurate use of the language of place value when carrying will support pupil progression and understanding.

"6 multiplied by 7 equals 42. Four tens and two units/ones"

Avoid 'carrying' stories such as 'put the milk bottles on the next door step' —

it is much more effective to use the language of place value.

t u
47
47 × 36

× 36

282 (47 × 6)

+
$$1410$$
 (47 × 30)

Optional additional notes

1692

Division			
Stage 1	Stage 2	Stage 3	
Pictures / marks 12 children get into teams of 4 to play a game. How many teams are there?			
	$\square \div \nabla = 3$ $3 = \square \div \nabla$ Understand division as sharing and grouping	Understand division as sharing and grouping Understanding division as repeated subtraction is key to understanding formal methods of division.	
The bead bar will help children with interpreting division calculations such as 10 ÷ 5 as 'how many 5s make 10?' 3 3 3 3 3 Use practical resources – cubes, counters, children etc	Grouping or repeated subtraction There are 6 sweets, how many people can have 2 sweets each? Repeated subtraction using a number line and bead bar $12 \div 3 = 4$ $0 1 2 3 4 5 6 7 8 9 10 11 12$	56÷8=7 Repeatedly subtract 8. Repeatedly subtract 8.	

Stage 4

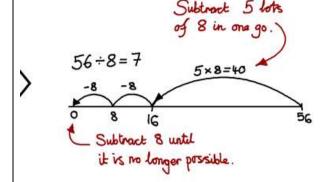
Stage 5 ÷ = signs and missing numbers

Division

Stage 6 ÷ = signs and missing numbers

÷ = signs and missing numbers

By using known times table facts shortcuts can be taken to reduce the number of steps needed to divide.



Division with remainders. $42 \div 8 = 5 \times 2$ Subtract 5 lots of 8. -8

Remainders

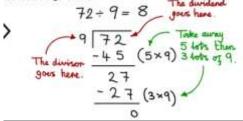
Quotients expressed as fractions or decimal fractions $61 \div 4 = 15 \frac{1}{4}$ or 15.25

Repeated subtraction using times table tacts.

Using known times table facts allows children to subtract larger 'chunka' from the original number. Children will be performing division where there are remainders.

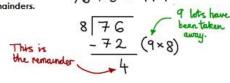
Chunking using times table tacts.

Once children are comfortable with division as repeated subtraction they can start to use more a more formal layout. When children are comfortable with the layout they can begin to use their ten times table to subtract in larger chunks.



Next Steps:

Chunking with remainders.



Remainders

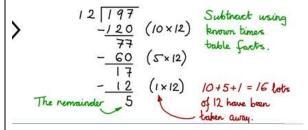
Quotients expressed as fractions or decimal fractions $676 \div 8 = 84.5$

Chunking using times table facts.

Children will continue to explore division as repeated subtraction. They will use their increasing knowledge of times tables to subtract in larger chunks. $|28 \div 7 = 18 \times 2$

Chunking using times table facts and multiples of 10.

Using their knowledge of the 10 times table will allow children to divide larger numbers by two-digit numbers while reducing the number of steps.



Expressing the remainder as a fraction.

$$50 \div 4 = 12 r^2$$
 The remainder

This can = $12^{2/4}$ The divisor. then be converted into a decimal.

Short division

98 ÷ 7 becomes

1 4 7 9 8

Answer: 14

432 ÷ 5 becomes

8 6 r 2 5 4 3 2

Answer: 86 remainder 2

496 ÷ 11 becomes

4 5 r1

1 1 4 9 6

Answer: $45\frac{1}{11}$

Long division

432 ÷ 15 becomes

Answer: 28 remainder 12

432 ÷ 15 becomes

$$\frac{12}{15} = \frac{4}{5}$$

Answer: $28\frac{4}{5}$

432 ÷ 15 becomes

Answer: 28-8